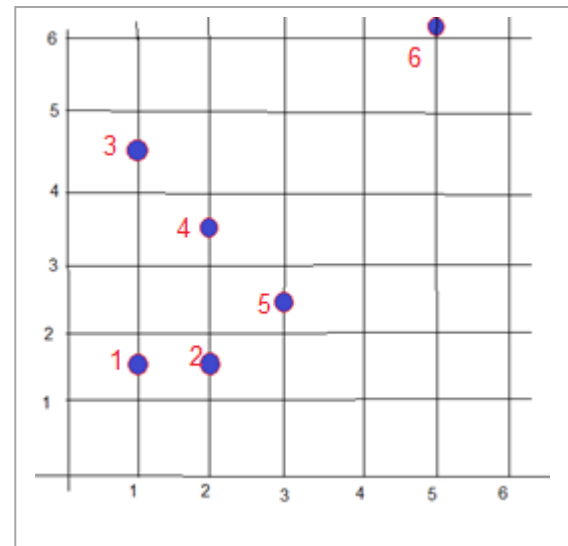


Consider the following instances [in the two-dimensional form]

Instance	X	Y
1	1.0	1.5
2	1.0	4.5
3	2.0	1.5
4	2.0	3.5
5	3.0	2.5
6	5.0	6.1



- If the Instances are to be partitioned into 2 clusters then take K=2.
- Next, choose two points at random representing initial cluster centres: Instance 1 and 3 are chosen as cluster centres; i.e. C1:= (1.0, 1.5) and C2:= (2.0, 1.5) are chosen as the initial centroid
- Evaluate distance between point i and j using Euclidean distance method

$$D(i - j) = \sqrt{(X_i - X_j)^2 + (Y_i - Y_j)^2}$$

- Initial cluster centres C1: (1.0, 1.5) C2: (2.0, 1.5)

- For Instance '1'

Distance between Cluster centre, C1(1.0, 1.5) and Instance1 (1, 1.5) is;

$$D(C1 - 1) = \sqrt{(1 - 1)^2 + (1.5 - 1.5)^2} = 0.00$$

Distance between Cluster centre C2(2.0, 1.5) and Instance1 (1, 1.5) is;

$$D(C2 - 1) = \sqrt{(2 - 1)^2 + (1.5 - 1.5)^2} = 1.00$$

Since  $D(C1-1) < D(C2-1)$  i.e. Instance1 is nearest from C1 than C2. So, the Instance '1' falls in cluster C1

- For Instance '2' (1.0,4.5) from C1(1.0, 1.5) and C2(2.0, 1.5)

$$D(C1 - 2) = 3.00; D(C2 - 2) = 3.16$$

Since  $D(C1-2) < D(C2-2)$  the Instance '2' falls in cluster C1

- For Instance '3' (2.0,1.5) from C1(1.0, 1.5) and C2(2.0, 1.5)

$$D(C1 - 3) = 1.00; D(C2 - 3) = 0.00$$

Since  $D(C2-3) < D(C1-3)$  the Instance '3' falls in cluster C2

- For Instance '4' (2.0,3.5) from C1(1.0, 1.5) and C2(2.0, 1.5)

$$D(C1 - 4) = 2.24; D(C2 - 4) = 2.00$$

Since  $D(C2-4) < D(C1-4)$  the Instance '4' falls in cluster C2

- For Instance '5' (3.0,2.5) from C1(1.0, 1.5) and C2(2.0, 1.5)

$$D(C1 - 5) = 2.24; D(C2 - 5) = 1.41$$

Since  $D(C2-5) < D(C1-5)$  the Instance '5' falls in cluster C2

- For Instance '6' (5.0,6.0) from C1(1.0, 1.5) and C2(2.0, 1.5)

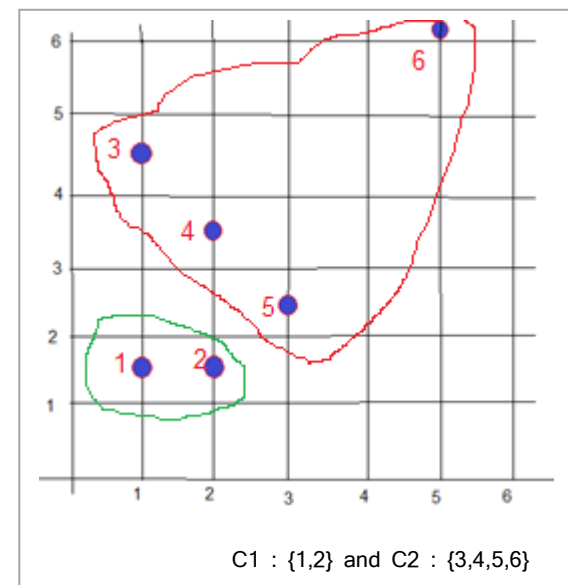
$$D(C1 - 6) = 6.02; D(C2 - 6) = 5.41$$

Since  $D(C2-6) < D(C1-6)$  the Instance '6' falls in cluster C2

- Then the cluster C1 and C2 contain the following Instances respectively

$$C1 : \{1,2\} \Rightarrow \{(1.0,1.5), (1.0,4.5)\}$$

$$C2 : \{3,4,5,6\} \Rightarrow \{(2.0,1.5), (2.0,3.5), (3.0,2.5), (5.0,6.0)\}$$



4. Recomputing cluster centers [taking the mean]

- a. for C1:

$$XC1 = (1.0+1.0)/2 = 1.0$$

$$YC1 = (1.5+4.5)/2 = 3.0$$

- b. For C2:

$$XC2 = (2.0+2.0+3.0+5.0)/4 = 3.0$$

$$YC2 = (1.5+3.5+2.5+6.0)/4 = 3.375$$

Thus the new cluster centers are C1(1.0,3.0) and C2(3.0,3.375)

5. As the cluster centers have changed the algorithm performs another iteration

- New cluster centers C1(1.0,3.0) and C2(3.0,3.375)

- D(C1 - 1) = 1.50 D(C2 - 1) = 2.74 Instance '1' falls in C1
- D(C1 - 2) = 1.50 D(C2 - 2) = 2.29 Instance '2' falls in C1
- D(C1 - 3) = 1.80 D(C2 - 3) = 2.13 Instance '3' falls in C1
- D(C1 - 4) = 1.12 D(C2 - 4) = 1.01 Instance '4' falls in C2
- D(C1 - 5) = 2.06 D(C2 - 5) = 0.88 Instance '5' will be in C2
- D(C1 - 6) = 5.00 D(C2 - 6) = 3.30 Instance '6' will be in C2

- Then the cluster C1 and C2 contain the following Instances respectively  
C1 : {1,2,3}  
C2 : {4,5,6}
6. computing new cluster centers [taking the mean]  
For C1:  $XC1 = (1.0+1.0+2.0)/3 = 1.33$   $YC1 = (1.5+4.5+1.5)/3 = 2.50$   
For C2:  $XC2 = (2.0+3.0+5.0)/3 = 3.33$   $YC2 = (3.5+2.5+6.0)/3 = 4.00$

Thus the new cluster centers are C1(1.33,2.50) and C2(3.33,4.3.00)

As the cluster centers have changed the algorithm performs another iteration

[repeat the process until there is no change in cluster centers or no Instance change its cluster]

